Mathematical studies of Feynman path integrals on Euclidean spaces is carried out by many mathematicians. However, there are only a few studies of those on manifolds due to difficulty caused by the global properties of manifolds. In this talk, I will talk on how to avoid this difficulty and construct fundamental solutions to Schrödinger equations on manifolds.